****King Fahd University of Petroleum & Minerals

College of Computer Science and Engineering

Information and Computer Science Department

Second Semester 132 (2013/2014)

ICS 202 – Data Structures

Final Exam

Sunday, May 18th, 2014

Time: 120 minutes

Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

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| Section 01 |  | Question # | Max Marks | Marks Obtained |
| Dr. Sami |  | 1 | 24 |  |
|  |  | 2 | 26 |  |
| Section 02 |  | 3 | 15 |  |
| Dr. Ramadan |  | 4 | 15 |  |
|  |  | 5 | 20 |  |
|  |  | Total | 100 |  |

**Instructions**

1. **Write your name and ID in the respective boxes above and circle your section.**
2. **This exam consists of 10 pages, including this page, plus one reference sheet, containing 6 questions.**
3. **You have to answer all 5 questions.**
4. **The exam is closed book and closed notes. No calculators or any helping aids are allowed.**
5. **Make sure you turn off your mobile phone and keep it in your pocket if you have one.**
6. **The questions are not equally weighed.**
7. **The maximum number of points for this exam is 100.**
8. **You have exactly 120 minutes to finish the exam.**
9. **Make sure your answers are readable.**
10. **If there is no space on the front of the page, feel free to use the back of the page. Make sure you indicate this in order not to miss grading it.**

**Q.1 [24 points] Multiple Choice Questions: Mark the best answer for each question below.**

**Note: only one choice should be chosen.**

1. Consider the following code segment

sum = 0;

for (j=1; j<=n; j++)

 for (k=1; k<=j; k++)

 sum++; // Statement 1

The complexity of the above code segment is

* 1. O (n2)
	2. O (n log n)
	3. O (n)
	4. O (log n)
	5. none of the above.
1. In the worst case searching an imbalanced Binary Search Tree is
	1. O (log n)
	2. O (n log n)
	3. O (n)
	4. O ($2^{n}-1$)
	5. none of the above.
2. The run-length encoding of the string EEESSSEEE:
	1. is ESE3.
	2. is E3S3E3.
	3. is 3ESE.
	4. can be both answers a and b.
	5. can be all answers a, b and c.
3. The postfix expression: 9 9 7 - - 3 4 + 8 6 - \* + evaluates to
	1. 0.
	2. – 25.
	3. – 7.
	4. 17.
	5. 21.
4. Consider the following AVL tree

The operation that **may** cause a single right rotation, without any double rotations on the AVL tree is:

* 1. inserting Key 48
	2. deleting Key 38
	3. deleting Key 45
	4. deleting Key 5
	5. none of the above
1. Consider the following directed graph

The number of strongly connected components is equal to

* 1. 5
	2. 4
	3. 3
	4. 2
	5. 1

**Q2. [26 points] (Graphs):**

* + - 1. Consider the following weighted directed graph GA(VA, EA, WA), where WA is the set of edge weights:



1. [4 points] Is it possible to solve the shortest path problem for the above graph? Justify your answer
2. [2 points] Is Dijkstra algorithm applicable on the above graph?
	* + 1. [10 points] Consider the weighted directed graph GA in the first part of the question, Let’s construct a new weighted directed graph GB (VB, EB, WB), where VB = VA , EB = EA , and WB is the absolute value of the corresponding value in WA. Apply Dijkstra algorithm to find the shortest path to any vertex starting from vertex s. Show the obtained tree of the shortest paths.

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Pass | initially |  |  |  |  |  | weight | Predecessor |
| ActiveVertex |  |  |  |  |  |
| s |  |  |  |  |  |  |  |  |
| u |  |  |  |  |  |  |  |  |
| v |  |  |  |  |  |  |  |  |
| x |  |  |  |  |  |  |  |  |
| y |  |  |  |  |  |  |  |  |

* + - 1. [10 points] Consider the following weighted undirected graph. Apply prim’s algorithm to find a minimum spanning tree of the graph starting from V7. Show the minimum spanning tree.



|  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Pass | initially |  |  |  |  |  |  |  | weight | V |
| ActiveVertex |  |  |  |  |  |  |  |
| V1 |  |  |  |  |  |  |  |  |  |  |
| V2 |  |  |  |  |  |  |  |  |  |  |
| V3 |  |  |  |  |  |  |  |  |  |  |
| V4 |  |  |  |  |  |  |  |  |  |  |
| V5 |  |  |  |  |  |  |  |  |  |  |
| V6 |  |  |  |  |  |  |  |  |  |  |
| V7 |  |  |  |  |  |  |  |  |  |  |

**Q3. [15 points]** (B+ Trees)

Consider the following B+ Tree where M=4 and L=5





Show the B+ Tree after each one of the following operations (note that all operations are independent, that is, in b perform the operation on the original B+ Tree, not the one obtained after performing the operation in a).

1. Delete(29)
2. Insert(6), Insert(7), Insert(8) (show only the B+ Tree after all 3 operations)

**Q4. [15 points]:** (Hashing)

Consider an open-addressing hash table of size 13 where the hash function is **h(Key)=Key % 13** and a second hash function is used for probing: **hp(Key) = 1 + Key % 12.**  Show the computation steps as well the final hash table when inserting the following values:

 14, 11, 17, 12, 27, 1, 40, 24, 53, 25

**Q5. [20 points]:** (Compression)

**Part A)** Huffman Coding

Assuming that a text file contains only the following characters with their corresponding frequencies:

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| **Character** | m | s | e | f | a | t |
| **Frequency** | 14 | 28 | 31 | 10 | 25 | 21 |

1. [7 points] Build the Huffman code tree for the text file message. You should show all the steps of the tree construction
2. [3 points] Use the Huffman tree to find the codeword for each character.
3. [5 points] What is the total number of bits of the compressed message? What is the compression ratio? Show your computations

**Part B)** Lempel-Ziv Compression

Compress the following message using LZ-78. (You must show the compression table):

BAABCAACCBAAABCA